Mathematical Representation of Students in Solving Mathematic Problems Reviewed from Extrovert-Introvert Personality

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ABSTRACT

In implementing mathematics learning in schools, educators must pay attention to five main competencies, namely problem solving, communication, connection, reasoning, and representation. Mathematical representation is a tool to convey students’ algebraic thinking as an aid to construct their ideas about patterns and functions. This study aims to examine the mathematical representation of students in terms of introvert and extrovert personality types. To see the characteristics of mathematical representations in solving mathematical problems when viewed from the personality type of each student. This research method is descriptive qualitative. The number of schools and students who were sampled from this study was taken using a multistage sampling technique. The data collection instruments in this study were personality questionnaires, problem-solving tests, interviews, observations, and documents obtained from research subjects. The problem-solving analysis used is based on the Krulik and Rudnik steps. The personality types of extroverted students and introverted students do have different mindsets so that even though in some steps they use the same representation, their tendencies or habits represent problem-solving using different forms of representation. The personality types of extroverted students represent them more symbolically and almost all answers from extroverted students are closer to true when compared to introverted students.

1. INTRODUCTION

National Council of Teacher of Mathematics (NCTM) states that in implementation of mathematics learning in school, educators must pay attention to the five main competency standards, that is problem solving, communication, connection, reasoning, and representation (Lee et al., 2018; Smith et al., 2018). In the process of learning mathematics, the ability to express and represent mathematical ideas is something that must be done by every person who learn mathematics (Cho & Tee, 2018; Ishak et al., 2020). In addition, function of mathematics is for developing of communication skills using numbers and symbols as well as sharpness of reasoning that can help solve problems in real life (Gurat, 2018; Ke & Clark, 2020).

Mathematical representation is a tool to convey students algebraic thinking as an aid to constructing their ideas about patterns and functions (Ratnasari et al., 2018; D. P. Sari, 2018). In the process of learning mathematics, the ability to express and represent mathematical ideas is something that must be done by every person who learn mathematics (Cho & Tee, 2018; Ishak et al., 2020). In addition, function of mathematics is for developing of communication skills using numbers and symbols as well as sharpness of reasoning that can help solve problems in real life (Gurat, 2018; Ke & Clark, 2020)

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Problem solving ability is the goal of learning mathematics, therefore problem solving abilities must be possessed by every students (Ningsih et al., 2020; Root et al., 2020). There are several types of problem solving in solving it, one of which is Krulik and Rudnick's steps. The problem solving steps by Krulik dan Rudnick are (1) read and think, (2) explore and plan, (3) select a strategy, (4) find an answer, and (5) reflect and extend. Each student has a different way of conveying, constructing, and solving a problem (Krulik & Rudnick, 1995). This difference shows the factors of different personality types among students, thus influencing students to convey, construct, and solve a problem. One way to solve this problem is to group them according to their creativity level to respect each student and not see them as simple on abilities than introverted individual.

Problem solving ability is an actor in the proposed research theme. In addition, in determining information, the snow ball sampling model can be used to expand the research subject. Respondents of this study were students in East Jakarta. Collecting data in this study were personality questionnaires, problem solving tests, mathematical problems through mathematical modeling (Gagatsis & Elia, 2004; Wieczorek & Lewandowski, 2017). This is also seen in the other results of research reveal that students' understanding and representation abilities are the key to getting the right problem solving solutions (Gagatsis & Elia, 2004; Zakris & Liljedah, 2004).

One of the internal factors that affect students' problem solving abilities is motivation and potential (Schmitt & Bradburn, 2018). Potential is a factor that students have that is closely related to their personality (Milliano, 2020; Yang & Li, 2018). The potential in students can be in the form of different personalities that can affect the thinking process. The character in the personality field, Jung, believed that when he knew the nature and direction of psychic energy in a person, he could indirectly know what he thought (Khorshidi, 2013). Therefore, by understanding and describing the inner feelings of an individual and presenting a descriptive frame of mind, the characteristics of a person can be determined more easily so that a deeper understanding can be obtained to increase self-awareness. Thus, the thought process will be related to the direction of psychic energy or personality that students have.

Jung suggested two personalities, namely extrovert and introvert personality (Samand et al., 2019; Yuliani et al., 2019). Based on research regarding the significant differences between extrovert and introvert individuals to simple reactions to conflict situations, it is concluded that introverted individuals who are focused and afraid of failure make them more careful, make fewer mistakes, but take more time to think (Burtăverde & Mihaila, 2011). In contrast, extrovert personalities respond more quickly but are prone to errors because they focus more on the environment rather than on themselves, extrovert individual have lower concentration abilities than introverted individual.

Extrovert personality is influenced by the objective world in the form of something outside himself (D. K. Sari et al., 2019; Suryabrata, 2007). Aspects of thoughts, feelings, and actions are determined by the environment, both social and non-social environment. Unlike the extrovert personality, the introvert personality is influenced by the subjective world of something within itself. Aspects of thoughts, feelings, and actions are determined by subjective factors. It can be concluded that extroverts-introverts have different sources of energy for their own individuals, so that there will be different thought processes that will be obtained from different aspects of the mind. Based on this, it can be said that different personalities are likely to produce different thought processes. This study discusses the mathematical representation of students in terms of introvert and extrovert personality types. In order to see the characteristics of mathematical representation in solving mathematical problems if seen from the personality type of each student.

2. METHOD

This research is a descriptive qualitative research. The number of schools and students who were sampled from this study was taken by using a multistage sampling technique. Meanwhile, to determine the research subject using the criterion-based selection model which is based on the assumption that the subject is an actor in the proposed research theme. In addition, in determining information, the snow ball sampling model can be used to expand the research subject. Respondents of this study were students in East Jakarta. Collecting data in this study were personality questionnaires, problem solving tests,
interviews, observations, and documents obtained from research subjects. Problem solving analysis used based on Krulik and Rudnick steps. They are are (1) read and think, (2) explore and plan, (3) select a strategy, (4) find an answer, and (5) reflect and extend (Krulik & Rudnick, 1995).

Data processing is carried out in several stages. The first stage of data processing starts from preliminary research to the compilation of research proposals. The second stage of data processing is carried out by processing the results of interviews and collecting various field information at the research location. The third stage is checking the validity of the data from interviews with a number of sources who are used as research informants and comparing the data with various related information. At this stage, data processing is considered optimal if the data obtained is considered complete and can represent the problem that is the object of research. The final stage is data analysis in order to answer the research questions carried out by using the triangulation analysis approach.

3. RESULT AND DISCUSSION

Result

After obtaining the results of the reduction in the field notes from the first, second and third data collection, the next step is to triangulate the time by comparing the results of the first, second, and third collection. Then obtained the same or valid data. If different data is obtained, the data is reduced. Based on the results of the analysis, there are similarities between the first data collection and the second data collection. From this similarity, it is obtained about the use of representations for students in solving problems in the linear equation material of two variables at each stage of Krulik and Rudnick. Table 1 shows the results of the analysis related to the forms of mathematical representations used by extrovert personality students and introverted personality students.

<table>
<thead>
<tr>
<th>Personality Types</th>
<th>Krulik and Rudnick steps</th>
<th>Problem Solving Description</th>
<th>Representation Form</th>
</tr>
</thead>
<tbody>
<tr>
<td>Extrovert</td>
<td>Read and Think</td>
<td>In this two stage position, students both use words to convey what is known and asked after writing first. How to convey too fast so it is not clear, only write down what is known.</td>
<td>Verbal</td>
</tr>
<tr>
<td></td>
<td>Explore and Plan</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Select and Strategy</td>
<td>In this stage, students use symbols to take the known information using x and y then write down the information in the form of linear equations correctly, the comparison formula, write the formula to determine the interest each month, then this formula is used to find the answer or the final result. how to operate a linear equation.</td>
<td>Symbolic</td>
</tr>
<tr>
<td></td>
<td>Find and Answer</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Introvert</td>
<td>Reflect and Extend</td>
<td>Students use symbols when asked about possible new problems. Students are less precise in conveying or changing the problem into the form of a mathematical model.</td>
<td>Symbolic</td>
</tr>
<tr>
<td></td>
<td>Read and Think</td>
<td>In these two stages, students convey what they know and are asked to use words slowly and clearly and correctly, write them completely and</td>
<td>Verbal and Visual</td>
</tr>
<tr>
<td></td>
<td>Explore and Plan</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Personality Types | Krulik and Rudnick steps | Problem Solving Description | Representation Form
---|---|---|---
Select and Strategy | then convey them by making tables first to make it easier to do, but in understanding them, students seem less focused. | Students convey in words and use the x and y symbols to take what is known and asked and write down the known information in the form of inaccurate linear equations, write the formula for determining the price. Students in substituting one equation for another are incomplete but the final answer is correct, such as determining x and y, determining the current number of problems with known logic into linear equations. | Verbal and Symbolic
Find and Answer | | | 
Reflect and Extend | Students convey in words and explanations, namely by reading the complete results of the solution and concluding linear equation problems and correctly when asked to rework with the same case but using different numbers. | Verbal dan Visual

Discussion
The use of various forms of representation (including verbal, visual, and symbolic representations) is an inseparable part of learning. This is in line with previous study that in constructing mathematical concepts, students must be able to construct in a way that can be understood by relating their ideas to meaningful articulations of various representations (Son, 2020; Supandi et al., 2018; Surya & Putri, 2017). In constructivism theory, students’ knowledge is the result of a construction from the students themselves. Knowledge is a cognitive construct that occurs through a series of one’s activities. The series of activities referred to involves the use of multiple representations. Based on the results of this study, the subject of extroverted personality (SE) shows the use of multiple representation in solving mathematical problems in Krulik and Rudnick's steps, namely in the Reflect and Extend step. The subject uses a form of visual and symbolic representation. Subjects are asked to solve problems that have been previously given in the mathematical model and be able to represent them. However, the results obtained by the SE subject’s graphic modeling are not accurate. Meanwhile, the subject of Introverted Personality (SI) shows that there is multiple representation in solving math problems in almost every step of Krulik and Rudnick. However, it appears that the use of visual representations is still lacking. This is because teachers rarely use visual representations when learning at school, so it requires additional time. This is in accordance with the research which revealed that The opinions of the students about the use of visual representations and the positive relationship between the use of visual representation and problem solving shows the need for teachers to give much more time to using visual representations in problem solving (Guler & Çıltas, 2011; Siagan et al., 2019; Simamora & Saragih, 2019).

The following describes the uses of extroverted personality (SE) students' mathematical representations in solving mathematical problems on linear equations. The use of mathematical representations of students in solving problems using Krulik and Rudnik's steps on linear equation material is known by giving students mathematical problems then asking them to solve these problems using Krulik and Rudnik's steps. There are three types of using the mathematical representation form of students in solving math problems. The three types include verbal representation, symbolic representation, and visual representation. The researcher used three indicators to determine the use of verbal representations, namely 1) writing down the steps to solve the problem using words; 2) conclude or answer questions using words. Indicators for symbolic representations include, 1) making mathematical equations or models from the given representation; 2) make a conjecture from a number; 3) solve the problem by involving mathematical expressions Furthermore, indicators in visual representations include, 1) using diagrams, tables or graphs to solve or conclude problems; 2) make pictures to clarify the problem and facilitate its resolution.
Then the subject is given questions that have never been done before or non-routine problems, to determine the use of mathematical representations of students in solving social arithmetic and comparison problems in representing problem solving based on Krulik and Rudnick's steps. In the Read and think step, almost all subjects (SE-1, SE-2, SE-3, SI-1, SI-2, SI-3) use verbal representations in describing what is known and asked. Likewise, in the Explore and Plan steps, the subject (SE-1, SE-2, SE-3) uses a verbal representation, for subjects SI-1 and SI-2 a visual representation is added. There is the use of symbolic representations by all SI subjects in the Select a Strategy step, while for SE subjects add verbal representations. There is the use of symbolic representations by all SE and SI subjects in the Find an Answer step, but the SI subjects are more consistent in using symbols while SE subjects are not consistent in their use of symbolic representations. Finally, there is the use of visual and symbolic representations by SI subjects, while SE subjects use verbal and visual representations in the Reflect and Extend step.

Based on the answers of three SE subjects and 3 SI subjects, it was found that SI subjects tended to represent mathematical problems using symbolic representations based on Krulik and Rudnick's steps, while SE subjects tended to represent mathematical problems using verbal representations based on Krulik and Rudnick's steps. SE and SI personality types do have different mindsets so that even though in several steps they use the same representation, the tendency to represent solving a problem uses different forms of representation. The SI personality type represents it symbolically and almost all the answers from the SI type are closer to being correct when compared to the SE type. This is in line with research which states that the extrovert personality is influenced by the objective world in the form of the world outside himself (Sanjaya et al., 2020; Suryabrata, 2007). Aspects of thoughts, feelings, and actions are determined by the environment, both social and non-social. The extrovert person is positive towards society as shown by his nature, namely his open heart, easy to socialize, and relationships with other people run smoothly. However, the weakness of the extrovert personality is that if the attachment to the outside world is too strong, then he will sink into the objective world and lose himself.

Previous research suggests that only a few students choose to use symbolic representations in communicating or conveying their mathematical ideas (Gagatsis & Elia, 2004; Guler & Çiltas, 2011; Supriadi et al., 2019). Students who focus on using algebraic (symbolic) representations describe students who have high abilities. This statement is in line with the fact that in this study the SI subject tends to represent a form of symbolic representation that has high abilities.

4. CONCLUSION

In the Read and Think and Explore and Plan steps, SE and SI students use verbal representations. SI students write down what they know and ask in advance in detail, and explain what is written. Meanwhile, SE students understand the problems that exist in the questions by describing them verbally, but are unable to write them in mathematical form. In the Select a Strategy and Find an Answer steps, SI students use symbolic representations by taking the known information using the x and y symbols and then writing the information into linear equations correctly as a mathematical model. Then the formula is used to find the answer or the final result by operating the algebraic equation, namely substituting one equation into another equation. Meanwhile, SE students can write the known information in the form of algebraic equations using symbols after being given several stages, then substitute one equation with another which is incomplete but the final answer is correct. In the Reflect and Extend step, SI students use a form of visual and symbolic representation when students are asked if the problem given is asked to change numbers. Then solve the problem in the same way as before. Meanwhile, SE students use verbal and visual representations by describing the method and logic of solving and concluding the problem correctly. Based on the use of students' mathematical representations in solving linear equation problems, it turns out that different representations are produced but tend to lead to certain forms of representation. This can be used as reference material for developing or conducting research related to the use of mathematical representations that have different characteristics.

5. ACKNOWLEDGEMENT

6. REFERENCES


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